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MOR and MOE of Serbian Spruce (*Picea omorika* Pančić/Purkyně) Wood from Natural Stands

Modul Ioma i modul elastičnosti drva omorike (*Picea omorika* Pančić/Purkyně) iz prirodnih sastojina

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ABSTRACT • The paper presents the results of testing the bending stress of Serbian spruce wood from natural stands. In testing the samples, in addition to the modulus of rupture, the bending stress at the proportionality limit, the ratio between the stress at the proportionality limit and the modulus of rupture as well as the modulus of elasticity of wood were determined. The study included nine trees from natural stands, and a total of 261 samples were tested. Regression analysis determined the dependences of these mechanical properties on the annual ring width, the proportion of late wood and wood density, as well as the dependence of the modulus of elasticity on the modulus of rupture.

Keywords: Picea omorika; modulus of rupture; modulus of elasticity; natural stands

SAŽETAK • U radu su prikazani rezultati ispitivanja naprezanja pri savijanju drva Pančićeve omorike podrijetlom iz prirodnih sastojina. Osim modula loma, pri ispitivanju uzoraka utvrđeni su i savojno naprezanje u točki proporcionalnosti, odnos čvrstoće na savijanje u točki proporcionalnosti i modula loma, kao i modul elastičnosti drva. Istraživanje je obuhvatilo devet stabala iz prirodnih sastojina, a ispitan je ukupno 261 uzorak. Regresijskom su analizom utvrđeni odnosi navedenih mehaničkih svojstava i širine goda, udjela kasnog drva i gustoće drva, kao i odnos modula elastičnosti i modula loma.

Ključne riječi: Picea omorika; modul loma; modul elastičnosti; prirodne sastojine

1 INTRODUCTION 1. UVOD

Serbian spruce (*Picea omorika* Pančić/Purkyně) is naturally distributed in Bosnia and Herzegovina and Serbia in the area around the middle and lower reaches of the Drina River. It is found on steep, rocky cliffs,

mostly on limestone, rarely serpentine, at altitudes of 300 to 1700 m (Vidaković and Franjić, 2004).

Serbian spruce is interesting from many aspects, both to the science and profession, and to the general public. A large number of scientific and professional papers deal with various issues related to Serbian

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spruce, ranging from its distribution, the configuration of the terrain as well as the habitat where it occurs (Fukarek, 1935, 1950; Čolić, 1953, 1957) to the latest genetic research (Aleksić and Geburek, 2010, 2014; Mataruga *et al.*, 2020). However, it is very difficult to find information in the literature concerning the mechanical properties of Serbian spruce wood, especially the wood originating from natural stands. Lukić-Simonović (1970) investigated in more detail the mechanical properties of Serbian spruce from its natural stands in western Serbia, while no such research has been done in Bosnia and Herzegovina.

Modulus of rupture (*MOR*) and modulus of elasticity (*MOE*) are among the most important parameters for determining the wood quality, especially for the usage of wood in construction (Bodig and Jayne, 1982). The modulus of elasticity, as a measure of stiffness, can be used to estimate strength because there is a positive correlation between stiffness and strength (Panshin and de Zeeuw, 1980). Popović (1990) states that the ratio between the bending stress at the proportionality limit and the modulus of rupture is a very important fact in the practical application of wood, where, if this ratio is known, the use of loads exceeding these values and leading to permanent deformation or fracture can be prevented.

Knowledge of the stress at the proportionality limit, maximum stress and their ratio, as well as the knowledge of the effect of certain factors on the specified bending characteristics has both scientific and practical significance. These factors are very important for designing the bending tools and for determination the stress that products can be exposed to during use (Svoboda *et al.*, 2017).

2 MATERIALS AND METHODS 2. MATERIJALI I METODE

The material for the research comes from three localities of the natural stands of Serbian spruce managed by the FE Panos - Višegrad. These are Gostilja (GO), Stolac 1 (S1) and Stolac 2 (S2). Location GO is at 1130 m above sea level, and the total area of this stand is 25.8 ha. S1 is located at 1200 m above sea level, and S2 at 960 m above sea level, while the total area of the stands is 29.5 ha.

According to Mataruga *et al.* (2011), Serbian spruce has been listed as an endangered plant species from 2010. Considering that, the selection of trees was taken into account when planning the research so that the relevant information was obtained with a minimum



Figure 1 Bending testing **Slika 1.** Ispitivanje svojstava pri savijanju

number of trees. From each locality, three trees were selected and harvested, and the average values of their characteristics by locations are given in Table 1.

Three logs, 1.2 m long, were cut from each tree. One log was taken from a height of 1.3 m, one from the part of the bole just below the first green branch, and one log was taken from the height in the middle between the two mentioned heights. From them, 30 mm thick radial planks were cut, out of which, after natural drying for three months and processing on the thickener, they were reduced to a thickness of 20 mm. From them, samples $(20 \text{ mm} \times 20 \text{ mm} \times 320 \text{ mm})$ for bending testing were made. The test was performed at the Material Testing Laboratory at the Faculty of Mechanical Engineering, University of Banja Luka, using a Messphysik "Beta 200", a universal testing machine used to test mechanical properties of different types of materials specialized in the testing of materials (Figure 1). The ISO 3133:1975 standard was used for bending testing.

For this test, 261 samples were selected. During selection, samples that are closest to the pith and that have natural defects were avoided. Before testing, the mass and dimensions in radial, tangential and axial directions of samples were measured. These data were used to calculate the wood density at the time of testing using Eq. 1:

$$\rho = \frac{m}{T \cdot R \cdot A} \cdot 1000 \left(\frac{g}{\text{cm}^3}\right) \tag{1}$$

Where:

m – sample mass at the time of testing (g)

T, R, A – sample dimensions in tangential, radial and axial direction at the time of testing (mm)

The samples were scanned in cross-section in order to determine the average annual ring width and the average proportion of late wood, using CDendro 7.6 and CooRecorder 7.6. Three-point bending tests were carried out to investigate the static behavior of sam-

Table 1 Average values of characteristics of Serbian spruce trees **Tablica 1.** Prosječne vrijednosti svojstava stabala Pančićeve omorike

| Location | Characteristics of trees / Svojstva stabala | | | | | | | | |
|------------------------------------|---|----------------|---|------|------------------|--|--|--|--|
| Location <i>Lokalitet</i> | Number of rings at 0.3 m | Tree height, m | Trunk length, m <i>Duljina debla</i> , m | | | | | | |
| Lokamet | Broj godova na 0,3 m Prsni promjer, cm | | | | Visina stabla, m | | | | |
| GO | 112 | 29.13 | 22.2 | 18.5 | | | | | |
| S1 | 131 | 30.00 | 28.4 | 24.4 | | | | | |
| S2 | 128 | 30.97 | 25.8 | 20.7 | | | | | |
| Average value Prosječna vrijednost | 124 | 30.03 | 25.4 | 21.2 | | | | | |

ples. Samples were placed so that they were on one radial side and the distance between the supports was 280 mm. The loading speed was set to 10 mm/min. Load-deflection graphs were obtained by testing and they were used to obtain the values of bending stress at the proportionality limit, MOR and MOE. The calculation formulas for MOR (Eq. 2) and bending stress at the proportionality limit (Eq. 3) are:

$$\sigma_s = \frac{3 \cdot F_{\text{max}} \cdot l}{2 \cdot b \cdot h^2} \text{ (MPa)}$$

$$\sigma_{\rm sp} = \frac{3 \cdot F_{\rm p} \cdot l}{2 \cdot h \cdot h^2} \text{ (MPa)}$$

Where:

 F_{max} – maximum load (N) F_{p} – load at proportionality limit (N) l – distance between supports (mm)

b – width of the sample (mm)

h – height of the sample (mm)

The calculation formula for MOE is:

$$E_{s} = \frac{F \cdot l^{3}}{4 \cdot b \cdot h^{3} \cdot f} \text{ (MPa)}$$

Where:

F – load from elastic zone (N)

l – distance between supports (mm)

b – width of the sample (mm)

h – height of the sample (mm)

f– deflection (mm).

The calculation formula for the ratio between the bending stress at the proportionality limit and MOR is:

$$P_{\sigma} = \frac{\sigma_{\rm sp}}{\sigma_{\rm s}} \cdot 100 \, (\%) \tag{5}$$

After the test, all samples were weighed and then dried to an oven dry state to determine moisture content at the time of testing using Eq. 6:

$$v_{\rm a} = \frac{m - m_0}{m_0} \cdot 100 \ (\%) \tag{6}$$

Where:

m – sample mass at the time of testing (g)

 $m_{\rm o}$ – sample mass in oven dry state (g)

In order to compare the obtained values of MOR and MOE with literature data, results of bending test were reduced to values at standard moisture content (12 %) using Eq. 7:

$$\sigma_{\rm s12}(E_{\rm sv}) = \sigma_{\rm sv}(E_{\rm sv}) \cdot [1 + 0.02 \cdot (v_{\rm a} - 12)] \,(\text{MPa})$$
 (7)

3 RESULTS AND DISCUSSION 3. REZULTATI I RASPRAVA

The average values of wood density and moisture content at the time of testing the samples from all three locations are given in Table 2. The average density of investigated Serbian spruce wood is 0.517 g/ cm³ at a moisture content of 15 %, while the average value of Serbian spruce wood density investigated by Lukić-Simonović (1955), from the territory of Serbia, at the same moisture content, was 0.482 g/cm³. The average annual ring width of investigated Serbian spruce wood is 1.76 mm and the average proportion of late wood is 15.24 %.

Table 3 shows the average values and other statistical indicators of MOR at standard moisture content by locations. Trees from GO have the lowest average values of MOR (84.23 MPa), and trees from S1 the largest (94.86 MPa). The smallest variation in MOR was found at S2 (12.19%) and the largest at GO (16.17%).

The average value of MOR at all locations (89.72) MPa) is slightly lower than the MOR at standard moisture content obtained in research by Lukić-Simonović (1970), namely 96.7 MPa. Studying the MOR of Serbian spruce wood from plantations in Germany, Kommert (1993) found that its average values at moisture content of 12 % are in the range of 57.6 MPa (average density of samples is 0.424 g/cm³) to 86 MPa (average density of samples is 0.510 g/cm³).

As the number of studies on the mechanical properties of Serbian spruce wood is limited, comparison with the mechanical properties of spruce wood was made. According to Karahasanović (1992), the MOR of spruce at a moisture content of (12 ± 3) % is 64 MPa. Gorišek *et al.* (2004) stated that the average *MOR* of spruce from Slovenia is 77.4 MPa, while Pushinskis et al. (2002) tested spruce from western Latvia and found that the average MOR is 106.42 MPa.

In addition to the MOR, the bending stress at the proportionality limit was determined, as well as the ratio between the bending stress at the proportionality limit and MOR. The obtained values are shown in Table 4 and 5.

The average bending stress at the proportionality limit for all three locations is 44.72 MPa, while the coefficient of variation is 15.92 %. The average ratio of

Table 2 Average values of annual rings width, proportion of late wood, density and moisture content of wood at the moment of testing

Tablica 2. Prosječne vrijednosti širine goda, udio kasnog drva, gustoće i sadržaja vode u drvu u trenutku ispitivanja

| Location | arw | plw | n | $v_{_{ m a}}$ | ρ | | |
|-----------|--------|-------|-----|---------------|-----------------------|-------|-------|
| Lokalitet | AV, mm | AV, % | " | AV, % | AV, g/cm ³ | SD, % | CV, % |
| S1 | 1.66 | 15.64 | 88 | 14.77 | 0.534 | 0.035 | 6.61 |
| S2 | 1.68 | 15.44 | 83 | 15.15 | 0.509 | 0.024 | 4.62 |
| GO | 1.90 | 14.80 | 90 | 15.30 | 0.508 | 0.028 | 5.54 |
| | 1.76 | 15.24 | 261 | 15.07 | 0.517 | 0.032 | 6.12 |

n – number of tested samples / broj testiranih uzoraka; v – moisture content at the moment of testing / sadržaj vode u trenutku ispitivanja; arw - annual ring width / širina goda; plw - proportion of late wood / udio kasnog drva; ρ - density of wood at the moment of testing / gustoća drva u trenutku ispitivanja; AV – average value / prosječna vrijednost; SD – standard deviation / standardna devijacija; CV – coefficient of variation / koeficijent varijacije

| Table 3 Statistical analysis of <i>MOR</i> of Serbian spruce from three different stem heights |
|--|
| Tablica 3. Statistička analiza modula loma Pančićeve omorike na uzorcima s tri različite visine debla |

| Location | Height of stem | n | | | $\sigma_{_{ m s}},$ | | |
|-----------|----------------|-----|---------|----------|---------------------|---------|-------|
| Lokalitet | Visina debla | " | AV, MPa | -95, MPa | +95, MPa | SD, MPa | CV, % |
| | I | 30 | 94.97 | 90.55 | 99.39 | 11.84 | 12.47 |
| S1 | II | 30 | 95.82 | 90.65 | 100.99 | 13.84 | 14.44 |
| 31 | III | 28 | 94.47 | 90.05 | 98.89 | 11.40 | 12.07 |
| | | 88 | 95.10 | 92.50 | 97.71 | 12.30 | 12.93 |
| | I | 25 | 84.61 | 78.37 | 90.84 | 15.11 | 17.86 |
| S2 | II | 31 | 94.61 | 92.46 | 96.76 | 5.87 | 6.20 |
| 32 | III | 27 | 89.59 | 86.09 | 93.08 | 8.84 | 9.87 |
| | | 83 | 89.96 | 87.56 | 92.37 | 11.01 | 12.24 |
| | I | 30 | 84.00 | 78.62 | 89.37 | 14.39 | 17.13 |
| GO | II | 30 | 84.13 | 80.40 | 87.87 | 9.99 | 11.88 |
| 30 | III | 30 | 84.55 | 78.50 | 90.60 | 16.20 | 19.16 |
| | | 90 | 84.23 | 81.37 | 87.08 | 13.62 | 16.17 |
| | | 261 | 89.72 | 88.12 | 91.32 | 13.14 | 14.64 |

 $\sigma_{\rm e}$ – modulus of rupture, $MOR \ / \ modul \ loma; n$ – number of tested samples $\ / \ broj \ testiranih \ uzoraka; AV$ – average value $\ / \ prosječna \ vrijednost;$ -95 – lower boundary of estimation interval with a probability of 95 % $\ / \ donja \ granica \ intervala \ procjene \ s \ vjerojatnošću od 95 %; +95$ – upper boundary of estimation interval with a probability of 95 % $\ / \ gornja \ granica \ intervala \ procjene \ s \ vjerojatnošću od 95 %; SD$ – standard deviation $\ / \ standardna \ devijacija; CV$ – coefficient of variation $\ / \ koeficijent \ varijacije$

the bending stress at the proportionality limit for all tested samples is 50.18 % of the maximum bending stress, while the variation is 12.73 %. Popović (1990) states that the bending stress at the proportionality limit for beech wood is on average 54.4 % and 56 % in the radial and tangential direction, respectively, from the value of the maximum bending stress.

Table 6 shows the average values of modulus of elasticity (*MOE*) at standard moisture content as well as other statistical parameters. The lowest average value of *MOE* was found in trees from GO (10953.99 MPa), and the highest in trees from S2 (12161.92 MPa). The smallest variation of *MOE* is at S2 (9.83 %) and the largest at S1 (21.46 %).

According to Šoškić and Popović (2002), the average value of *MOE* for spruce is 11000 MPa, which is approximately the value of *MOE* for Serbian spruce

obtained in this study (11566.23 MPa). Johansson and Kliger (2000) state that the average value of MOE determined from bending for spruce is 12500 MPa, according to Aanerød (2014) 12800 MPa, with a coefficient of variation of 19.5 %, while according to Pushinskis *et al.* (2002) it is 13660 MPa.

Analysis of the variance of *MOR* showed that there is statistically significant difference between the locations, while there is no difference between the locations in the ratio between bending stress at the proportionality limit and *MOR*. Using the Duncan test in the analysis of the variance of MOE, the locations were classified into two homogeneous groups, i.e. it was noticed that there is no statistically significant difference between the locations S1 and S2. In the analysis of the variance of the bending stress at the proportionality limit, locations were classified into two homogeneous

Table 4 Statistical analysis of bending stress at proportionality limit of Serbian spruce from three different stem heights **Tablica 4.** Statistička analiza savojnog naprezanja u točki proporcionalnosti Pančićeve omorike na uzorcima s tri različite visine debla

| Location | Height of stem | 14 | $\sigma_{ m sp}$ | | | | | | | |
|-----------|----------------|-----|------------------|----------|----------|---------|-------|--|--|--|
| Lokalitet | Visina debla | n | AV, MPa | -95, MPa | +95, MPa | SD, MPa | CV, % | | | |
| | I | 30 | 49.67 | 47.04 | 52.31 | 7.06 | 14.20 | | | |
| S1 | II | 30 | 47.10 | 44.00 | 50.20 | 8.30 | 17.63 | | | |
| 51 | III | 28 | 47.85 | 46.14 | 49.55 | 4.40 | 9.20 | | | |
| | | 88 | 48.21 | 46.76 | 49.66 | 6.84 | 14.19 | | | |
| | I | 25 | 42.73 | 40.27 | 45.20 | 5.98 | 13.99 | | | |
| S2 | II | 31 | 45.45 | 43.57 | 47.33 | 5.13 | 11.29 | | | |
| 52 | III | 27 | 42.78 | 40.45 | 45.11 | 5.89 | 13.78 | | | |
| | | 83 | 43.76 | 42.51 | 45.01 | 5.73 | 13.09 | | | |
| | I | 30 | 41.17 | 38.64 | 43.70 | 6.77 | 16.45 | | | |
| CO | II | 30 | 41.47 | 38.77 | 44.16 | 7.22 | 17.41 | | | |
| GO | III | 30 | 43.89 | 41.03 | 46.76 | 7.67 | 17.46 | | | |
| | | 90 | 42.18 | 40.66 | 43.70 | 7.25 | 17.19 | | | |
| | | 261 | 44.72 | 43.85 | 45.58 | 7.12 | 15.92 | | | |

 $[\]sigma_{\rm sp}$ – bending stress at proportionality limit / savojno naprezanje u točki proporcionalnosti, n – number of tested samples / broj testiranih uzoraka; AV – average value / prosječna vrijednost; -95 – lower boundary of estimation interval with a probability of 95 % / donja granica intervala procjene s vjerojatnošću od 95 %; +95 – upper boundary of estimation interval with a probability of 95 % / gornja granica intervala procjene s vjerojatnošću od 95 %; SD – standard deviation / standardna devijacija; CV – coefficient of variation / koeficijent varijacije

Table 5 Statistical analysis of ratio between bending stress at proportionality limit and *MOR* of Serbian spruce from three different stem heights

Tablica 5. Statistička analiza odnosa savojnog naprezanja u točki proporcionalnosti i modula loma Pančićeve omorike na uzorcima s tri različite visine debla

| Location | Location Height of stem | | | | | | |
|-----------|-------------------------|-----|-------|-------|-------|------|-------|
| Lokalitet | Visina debla | n | AV | -95 | +95 | SD | CV |
| | I | 30 | 52.35 | 50.82 | 53.87 | 4.08 | 7.80 |
| S1 | II | 30 | 49.16 | 47.41 | 50.92 | 4.70 | 9.57 |
| 51 | III | 28 | 51.14 | 48.92 | 53.36 | 5.73 | 11.20 |
| | | 88 | 50.88 | 49.82 | 51.94 | 4.99 | 9.81 |
| | I | 25 | 51.61 | 48.00 | 55.22 | 8.75 | 16.95 |
| S2 | II | 31 | 48.01 | 46.49 | 49.53 | 4.15 | 8.64 |
| 52 | III | 27 | 47.82 | 45.77 | 49.87 | 5.18 | 10.84 |
| | | 83 | 49.03 | 47.65 | 50.42 | 6.33 | 12.92 |
| | I | 30 | 49.53 | 46.85 | 52.20 | 7.16 | 14.45 |
| CO | II | 30 | 49.50 | 46.51 | 52.49 | 8.00 | 16.17 |
| GO | III | 30 | 52.67 | 50.04 | 55.31 | 7.07 | 13.42 |
| | | 90 | 50.57 | 49.00 | 52.14 | 7.49 | 14.81 |
| | | 261 | 50.18 | 49.41 | 50.96 | 6.39 | 12.73 |

 P_{σ} – ratio between bending stress at proportionality limit and MOR / odnos savojnog naprezanja u točki proporcionalnosti i modula loma; n – number of tested samples / broj testiranih uzoraka; AV – average value / prosječna vrijednost; -95 – lower boundary of estimation interval with a probability of 95 % / donja granica intervala procjene s vjerojatnošću od 95 %; +95 – upper boundary of estimation interval with a probability of 95 % / gornja granica intervala procjene s vjerojatnošću od 95 %; SD – standard deviation / standardna devijacija; CV – coefficient of variation / koeficijent varijacije

Table 6 Statistical analysis of *MOE* of Serbian spruce from three different stem heights **Tablica 6.** Statistička analiza modula elastičnosti Pančićeve omorike na uzorcima s tri različite visine debla

| Location | Height of stem | n | $E_{_{\mathrm{S}}}$ | | | | | | |
|-----------|------------------|-----|---------------------|----------|----------|---------|-------|--|--|
| Lokalitet | tet Visina debla | " | AV, MPa | -95, MPa | +95, MPa | SD, MPa | CV, % | | |
| | I | 24 | 11267.32 | 10400.02 | 12134.63 | 2053.95 | 18.23 | | |
| S1 | II | 27 | 12182.87 | 11216.82 | 13148.92 | 2442.07 | 20.05 | | |
| 31 | III | 26 | 11442.37 | 10597.84 | 12286.91 | 2090.90 | 18.27 | | |
| | | 77 | 11647.47 | 11144.18 | 12150.76 | 2529.33 | 21.46 | | |
| | I | 25 | 11699.33 | 11118.42 | 12280.24 | 1407.31 | 12.03 | | |
| S2 | II | 30 | 12625.86 | 12240.59 | 13011.12 | 1031.75 | 8.17 | | |
| 32 | III | 27 | 12074.75 | 11684.79 | 12464.71 | 985.78 | 8.16 | | |
| | | 82 | 12161.92 | 11899.33 | 12424.50 | 1195.06 | 9.83 | | |
| | I | 30 | 10674.33 | 10053.79 | 11294.88 | 1661.86 | 15.57 | | |
| CO | II | 30 | 10879.25 | 10313.77 | 11444.72 | 1514.37 | 13.92 | | |
| GO | III | 30 | 11308.40 | 10649.02 | 11967.78 | 1765.85 | 15.62 | | |
| | | 90 | 10953.99 | 10607.69 | 11300.29 | 1653.42 | 15.09 | | |
| | | 249 | 11566.23 | 11342.61 | 11789.85 | 1791.57 | 15.49 | | |

 E_s — modulus of elasticity (MOE) / modul elastičnosti, n — number of tested samples / broj testiranih uzoraka; AV — average value / prosječna vrijednost; -95 — lower boundary of estimation interval with a probability of 95 % / donja granica intervala procjene s vjerojatnošću od 95 %; +95 — upper boundary of the estimation interval with a probability of 95 % / gornja granica intervala procjene s vjerojatnošću od 95 %; SD — standard deviation / standardna devijacija; CV — coefficient of variation / koeficijent varijacije

Table 7 Analysis of variation of *MOR*, *MOE*, bending stress at proportionality limit, ratio between bending stress at proportionality limit and *MOR*

Tablica 7. Analiza varijance modula loma, modula elastičnosti i savojnog naprezanja na granici proporcionalnosti te odnosa savojnog naprezanja na granici proporcionalnosti i modula loma

| | | Location / Lokalite | ANOVA | | | |
|-------------------------|--------------------|---------------------|-----------------------|-------|--------|-----------|
| | S1 | S2 | GO | F | p | Post-hoc* |
| $\sigma_{\rm s}$, MPa | 95.10° | 89.96 ^b | 84.23ª | 17.16 | 0.0000 | 3 |
| $E_{\rm s}$, MPa | 11647,47ª | 12161.92ª | 10566.23 ^b | 8.18 | 0.0004 | 2 |
| $\sigma_{\rm sp}$, MPa | 48.21 ^b | 43.76ª | 42.18a | 19.53 | 0.0000 | 2 |
| P ₀ , % | 50.88a | 49.03ª | 50.57a | 2.04 | 0.1320 | 1 |

^{*}Number of homogeneous groups by Duncan's test / broj homogenih grupa prema Duncanovu testu

a, b, c Homogeneous groups / homogene grupe

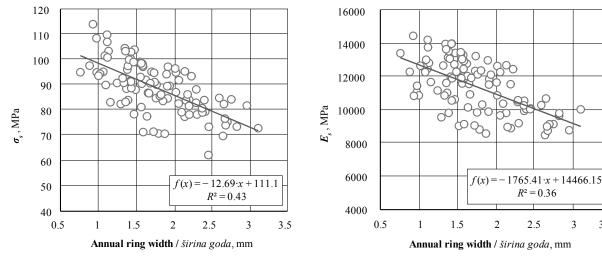


Figure 2 Dependence of MOR and MOE on annual ring width Slika 2. Ovisnost modula loma i modula elastičnosti o širini goda

groups, i.e. the analysis showed that there is no statistically significant difference between sites S2 and GO (Table 7).

In addition to wood density, which is considered to be the most significant factor affecting wood properties, the influence of compression and juvenile wood, the angle of the microfibrils and the width of the growth ring, which have the same, if not greater, influence on the wood properties, should not be neglected (Alteryac et al., 2006). The influence of the annual ring width on the MOR and MOE can be seen in Figure 2. According to Roemer-Orphal table for determining the strength of correlation dependence (according to Vasilj, 2000), there is a strong negative correlation between these parameters.

Proportion of late wood has a positive effect on MOR and MOE (Figure 3). Based on the correlation coefficients, it can be concluded that the correlation is moderate.

The dependence of MOR on wood density has been tested by a number of researchers. Thus, Schlyter (1927) states that this dependence is linear, while according to Baumann (1922) it is curvilinear. In any

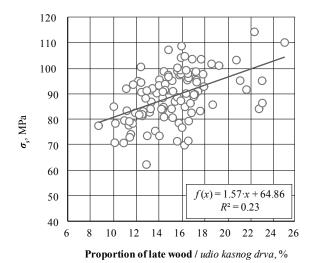
case, as the density of wood increases, the bending strength also increases, which is confirmed by this research (Figure 4). As wood density of Serbian spruce grows, so does the modulus of elasticity, although these correlations are slightly smaller than the correlations between density and MOR. In their study, Raiskila et al. (2006) state that the same is the case with spruce wood.

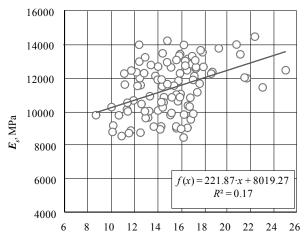
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3 5

In order to obtain a model for strength estimation, the regression analysis included the dependence of MOR on annual ring width and wood density. Multiple regression equation (Function 8) was obtained by stepwise multiple regression method. The parameters of the obtained equation and the regression characteristics (Table 8) show that there is a pronounced dependence of MOR on the included elements. All regression coefficients are statistically significant at the p < 0.001level, as is the regression as a whole. On the basis of the coefficient of determination, 33 % of the variation of the MOR value is explained by the variation of the observed elements.

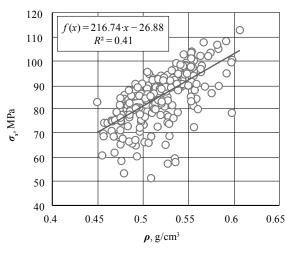
$$\sigma_s = a + b \cdot arw^2 + c \cdot \rho^2 \tag{8}$$





Proportion of late wood / udio kasnog drva, %

Figure 3 Dependence of MOR and MOE on proportion of late wood Slika 3. Ovisnost modula loma i modula elastičnosti o udjelu kasnog drva



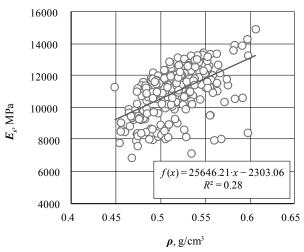


Figure 4 Dependence of *MOR* and *MOE* on wood density at the moment of testing **Slika 4.** Ovisnost modula loma i modula elastičnosti o gustoći drva u trenutku ispitivanja

Generally, the *MOE* is considered the most important strength predictor parameter (Baar *et al.*, 2015). Investigating the correlation between *MOR* and *MOE* in spruce, Johansson and Kliger (2000) found that the coefficient of determination was 0.51. The equation of relation between bending strength and modulus of elasticity reported by Johansson *et al.* (1992) is:

$$\sigma_s = 0.00383 \cdot E_s - 2.4 \tag{9}$$

The dependence of *MOR* on *MOE* examined in this paper can be seen in Figure 5. The correlation is

linear and positive, and based on the correlation coefficient of 0.77, it can be concluded that the correlation is very strong.

4 CONCLUSIONS 4. ZAKLJUČAK

The results obtained in this paper have substantially improved the knowledge of certain mechanical properties of Serbian spruce from the territory of Bosnia and Herzegovina. It can be observed that Serbian spruce

Table 8 Regression characteristics (dependence of *MOR* on annual ring width and wood density at the moment of testing) **Tablica 8.** Obilježja regresije (ovisnost modula loma o širini goda i gustoći drva u trenutku ispitivanja)

| Regression coefficient Koeficijent regresije | | Std. Err. of coeff. Standardna pogreška koeficijenta | t | p | S _e , mm | R | R^2 | F | p | n |
|--|----------|--|----------|----------|---------------------|------|-------|----------|--------|-----|
| a | 60.1964 | 10.77431 | 5.58703 | 0.000000 | | | | | | |
| b | -2.0408 | 0.56226 | -3.62969 | 0.000453 | 9.25774 | 0.58 | 0.33 | 25.42762 | 0.0000 | 101 |
| c | 111.4477 | 36.67212 | 3.03903 | 0.003043 | | | | | | |

 $S_{\rm e}$ – standard error of regression / standardna pogreška regresije, R – correlation coefficient / koeficijent korelacije, R^2 – determination coefficient / koeficijent determinacije

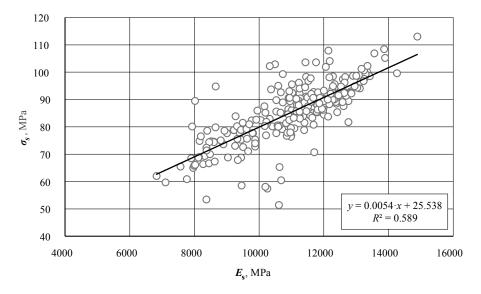


Figure 5 Dependence of *MOR* on *MOE* **Slika 5.** Ovisnost modula loma o modulu elastičnosti

has quite high values of *MOR* and *MOE*. Serbian spruce is known to be a protected species and not industrially significant. However, given its good mechanical properties, consideration should be given to establishing larger surfaces of planted forests with the aim of using Serbian spruce wood as a technical wood. Since there is a correlation between the width of the annual rings and *MOR*, care should be taken to achieve optimum growth in establishing and managing the new forest.

The modulus of elasticity may be a good predictor for determining the bending strength, given the very strong correlation between these two parameters.

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